

(Lecture 6) Boolean Algebra

Laws:-

- i) $x + 0 = x$
- ii) $x \cdot 0 = 0$
- iii) $x + 1 = 1$
- iv) $x + x = x$
- v) $x \cdot x = x$
- vi) $x' \cdot 0 = 0$
- vii) $x' \cdot 1 = x'$
- viii) $x'y + xy' = x \oplus y$

Involution:- $(x')' = x$

Commutative:-

- a) $x + y = y + x$
- b) $x \cdot y = y \cdot x$

Associative:-

- a) $x + (y + z) = (x + y) + z$
- b) $x \cdot (y \cdot z) = (x \cdot y) \cdot z$

Distributive

$$x(y + z) = x \cdot y + x \cdot z$$

$\frac{13}{11}$

1) De-Morgan's Law:-

$$i) (x+y)' = x' \cdot y'$$

$$ii) (\overline{x \cdot y}) = x' + y'$$

Absorption Law:-

$$x + xy = x$$

x	y	x'	y'	x+y	x·y	x'+y'
0	0	1	1	0	0	1
0	1	1	0	1	0	1
1	0	0	1	1	0	0
1	1	0	0	1	1	1

Question:- $x + xy = x$

L.H.S

$$= x + xy$$

$$= x(1+y)$$

$$= x \cdot 1 = x \quad \text{proved}$$

Question:-

$$= x' + xy' + x'y'$$

$$= x'(1+y) + x'y'$$

$$= x'(1) + xy'$$

$$= x' + xy'$$