

(Lecture 9.10) Events:-

- An event is a subset of Sample Space.
- Particular outcome which is in my interest.

Example:- If we throw a dice & interest is in divisible by 3.
then event is $A = \{3, 6\}$

Complement of S.S = $A = A' = \{1, 2, 4, 5\}$

→ Mutual Exclusive or Disjoint

$$A \cap B = \emptyset$$

→ If $A = \{1, 4, 6\}$, $B = \{1, 3, 5\}$ ∴ They don't interfere each other, don't affect each other

$$A \cap B = \{ \}$$

→ If $A = \{1, 3, 5\}$, $B = \{3, 5\}$

$$A \cap B = \{3, 5\} \text{ . Not disjoint}$$

→ Union:-

$$A \cup B = \{1, 3, 5\}$$

• Counting Sample points:-

Theorem 2.1:- (Multiplication Rule)

• A Dice and A Coin

$$n_1 = 6 \text{ ways} \quad , \quad n_2 = 2 \text{ ways}$$

$$n_1 \cdot n_2 = 12 \text{ ways}$$

Theorem 2.2:- more than
if we have two values.

$$n_1 \cdot n_2 \cdot n_3 \cdot n_4 \dots = ?$$

Example 2.10:-

→ 0, 1, 2, 5, 6 and 9
write four digit even number.
find out possibilities?

Case 1:- For 0 at Unit

Tho. Hun. Ten Unit
4 4 3 0

$$n_1 = 1, n_2 = 5, n_3 = 4, n_4 = 3 = 1 \cdot 5 \cdot 4 \cdot 3 = 60$$

Case 2:- For (2, 6) at Unit

Tho. Hun. Ten Unit

$$= 4 \cdot 4 \cdot 3 \cdot 2 = 96$$

$$n_2 = 4, n_3 = 4, n_4 = 3, n_1 = 2$$

$$\text{Total possibilities} = 60 + 96 = \underline{156}$$

Definition 2.7:-

Arrangement of Elements:-

abc

Arrange them to all possibilities:-

a, b, c
a, c, b
b, c, a
b, a, c
c, a, b
c, b, a

$$4 \cdot 3 \cdot 2 \cdot 1 = 6$$

$$\text{Formula} = n(n-1)(n-2) = 6$$

$$\downarrow$$

$$n! = 3!$$

Date:

If we want to find Arrangement for 2 Digits from four then we will count upto 2!

$$\frac{n!}{(n-r)!} = \frac{4!}{(4-2)!} = \frac{4!}{2!} = \frac{4 \cdot 3 \cdot 2 \cdot 1}{2 \cdot 1} = 12$$

Theorem 2.4:-

Formula:- $nPr = \frac{n!}{(n-r)!}$

Example- If we want to divide 3 Awards Among 40 graduates!

$$\frac{40!}{(40-3)!} = \frac{40!}{37!} = \frac{40 \cdot 39 \cdot 38 \cdot 37!}{37!} = 59280$$

→ In case of Circle, we will count factorial upto (n-1) from 1st. Formula:- $(n-1)!$

Example 8 people are sitting in circle. Find out possible Arrangements?

We will calculate = 7!

Theorem 2.6:- If we want to divide in groups-

$$\text{Formula} = \frac{n!}{n_1! \cdot n_2! \cdot n_3!}$$

Example.. Divide 10 Students in 3 groups.

$$\frac{10!}{3! \cdot 3! \cdot 4!} = ?$$

niceday

Date:

Combination:-

Order & Arrangement does not matters.

Object = n
at a time $r = 2$

$${}^n C_r = \frac{n!}{r!(n-r)!}$$

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